

Analysis of Leaky Deception for Network Security using Signaling Games with Evidence

Jeffrey Pawlick, Edward Colbert, and Quanyan Zhu

Abstract

Deception plays critical roles in economics and technology, especially in emerging interactions in cyberspace. Holistic models of deception are needed in order to analyze interactions and to design mechanisms that improve them. Game theory provides such models. In particular, existing work models deception using signaling games. But signaling games inherently model deception that is undetectable. In this paper, we analyze an extended version of signaling games that includes a detector which gives off probabilistic warnings when the sender acts deceptively. We derive pooling and partially-separating equilibria of the game. We find that 1) high-quality detectors eliminate some pure-strategy equilibria, 2) detectors with high true-positive rates encourage more honest signaling than detectors with low false-positive rates, and 3) receivers obtain optimal outcomes for equal-error-rate detectors. We illustrate these results with an application to defensive deception for network security. Our results provide a quantitative and rigorous analysis of the fundamental aspects of detectable deception.

Index Terms

Deception, game theory, signaling game, trust management, strategic communication

I. INTRODUCTION

Deception is a fundamental facet of interactions ranging from biology [7] to criminology [40] and from economics [14] to the Internet of Things (IoT) [35]. Cyberspace creates particular opportunities for deception, since information is transient, imputing responsibility is difficult [21], and agents lack repeated interactions [28]. For instance, online interactions are vulnerable to identity theft [17] and spear phishing [1], and authentication in the IoT suffers from a lack of local computational resources [3].

Defenders also implement deception. Traditional security approaches such as firewalls and role-based access control (RBAC) have proved insufficient against insider attacks and advanced persistent threats (APTs). Hence, defenders in the security and privacy domains have proposed, *e.g.*, honeynets [5], moving target defense [44], obfuscation [33], and mix networks [42]. Using these techniques, defenders can

Author Contact Information—Jeffrey Pawlick (jpawlick@nyu.edu) and Quanyan Zhu (quanyan.zhu@nyu.edu): Department of Electrical and Computer Engineering, New York University Tandon School of Engineering, 5 MetroTech Center, Brooklyn, NY 11201. Edward Colbert (edward.j.colbert2.civ@mail.mil) and Jeffrey Pawlick: Computational and Information Sciences Directorate, U.S. Army Research Laboratory, 2800 Powder Mill Road, Adelphi, MD 20783.

This work is partially supported by an NSF IGERT grant through the Center for Interdisciplinary Studies in Security and Privacy (CRISSP) at New York University, by the grant CNS-1544782, EFRI-1441140, and SES-1541164 from National Science Foundation (NSF) and DE-NE0008571 from the Department of Energy. Research was also sponsored by the Army Research Laboratory and was accomplished under Cooperative Agreement Number W911NF-17-2-0104. The views and conclusions contained in this document are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of the Army Research Laboratory or the U.S. Government. The U.S. Government is authorized to reproduce and distribute reprints for Government purposes notwithstanding any copyright notation herein.

obscure valuable data such as personally identifiable information or the configuration of a network. They can also send false information to attackers in order to waste their resources or attract them away from critical assets. Both malicious and defensive deception have innumerable implications for cybersecurity.

A. Quantifying Deception using Signaling Games

Modeling deceptive interactions online and in the IoT would allow government policymakers, technological entrepreneurs, and vendors of cyber-insurance to predict changes in these interactions due to legislation, new technology, or risk mitigation. While deception is studied in each of these domains individually, a general, quantitative, and systematic understanding of deception seems to be lacking.

What commonalities underlie all forms of deception? Deception is 1) information asymmetric, 2) dynamic, and 3) strategic. In deceptive interactions, one party (hereafter, the *sender*) possesses private information unknown to the other party (hereafter, the *receiver*). Based on her private information, the sender communicates a possibly-untruthful message to the receiver. Then the receiver forms a belief about the private information of the sender, and chooses an action. The players act *strategically*, in the sense that they each seek a result that corresponds to their individual incentives.

Non-cooperative game theory provides a set of tools to study interactions between multiple, strategic agents. In the equilibrium of a game, agents adapt their strategies to counter the strategies of the other agents. This rationality models the sophisticated behavior characteristic of deception. In particular, *cheap-talk signaling games* [9] model interactions that are strategic, dynamic, and information-asymmetric. In cheap-talk signaling games, a sender S with private information communicates a message to a receiver R , who acts upon it. Then both players receive utility based on the private information of S and the action of R . Recently, signaling games have been used to model deceptive interactions in resource allocation [45], cyber-physical systems [31], [43], and network defense [5].

B. Cost and Detection in Signaling Games

The phrase *cheap talk* signifies that the utility of both players is independent of the message that S communicates to R . In cheap-talk signaling games, therefore, there is no cost or risk of lying *per se*. Truth-telling sometimes emerges in equilibrium, but not through the penalization or detection of lying. We can say that cheap-talk signaling games model deception that is *undetectable* and *costless*. Meanwhile, models by Hendricks and McAfee [19] and Kartik [23] study deception that is *costly*. S pays an explicit cost to send a message that does not truthfully represent her private information. Yet the deception is still undetectable.

In many scenarios, however, deception can be detected with some probability. Consider the issue of so-called *fake news* in social media. Fake news stories about the 2016 U.S. Presidential Election reportedly received more engagement on Facebook than news from real media outlets [38]. In the wake of the election, Facebook announced its own program to detect fake news and alert users about suspicious articles. As another example, consider deceptive product reviews in online marketplaces. Linguistic analysis has been used to detect this *deceptive opinion spam* [30]. Finally, consider deployment of honeypots as a technology for defensive deception. Attackers have developed tools that detect the virtual machines often used to host honeypots.

Therefore, we analyze a model of signaling games in which a detector emits probabilistic evidence of deception. The detector can be interpreted in two equally valid ways. It can be understood as a technology that R uses to detect deception, such as a phishing detector in an email client. Alternatively, it can be understood as the inherent tendency of S to emit cues to deception when she misrepresents her private information. For instance, in interpersonal deception, lying is cognitively demanding, and sometimes liars give off cues from these cognitive processes [40]. R uses the evidence from the detector to form a belief about whether S 's message honestly conveys her private information.

C. Model Overview

Let us consider an informal overview of the model. S has a private bit of information that is either 0 or 1. S can either transmit the true bit to R , or S can run a program that deceptively sends the opposite bit to R . With some probability, however, R can detect the running of the deceptive program. In that case, we say that the detector gives off an alarm. The detector is imperfect and can also give off false alarms. Based on the bit sent by S and the evidence emitted by the detector (alarm or no alarm), R attempts to guess the private bit. R receives a higher utility if he is correct than if he is wrong, and S receives a higher payoff if R is wrong than if he is correct.

Naturally, several questions arise. What is the equilibrium of the game? How, if at all, is the equilibrium different than that of a traditional cheap-talk signaling game? Is detection always harmful for the sender? Finally, how does the design of the detector affect the equilibrium? Our paper addresses each of these questions.

D. Contributions

We present the following contributions:

- 1) We find all pure-strategy equilibria of cheap-talk signaling games with evidence.
- 2) We derive mixed-strategy equilibria in regimes that do not support pure-strategy equilibria.
- 3) We prove that detectors that prioritize high true-positive rates encourage more honest signaling than detectors that prioritize low false-positive rates. We also show that receivers prefer equal-error-rate detectors.
- 4) We apply our analytical results to a case study in defensive deception for network security, and show that both players' equilibrium strategies are robust to sub-optimal deviations of the other player.

E. Related Work

Signaling games with evidence are related to the general areas of *hypothesis testing* and *inspection games*. Hypothesis testing is used to evaluate the truthfulness of claims based on probabilistic evidence [25]. Inspection games embed a hypothesis testing problem inside of a two-player game [4]. An *inspector* designs an inspection technique in order to motivate an *inspectee* to follow a rule or regulation. Our work adds the concept of signaling to the framework of inspection games.

Our work builds upon Crawford and Sobel's original formulation of cheap-talk games [9]. In this paper, a sender can just as easily (exogenously) misrepresent her private information as truthfully represent it.

From the opposite vantage point, models from Milgrom [27], Grossman [15], and Grossman and Hart [16] study games of verifiable disclosure. In these models, if a sender chooses to disclose information, then she must do so truthfully.

Hendricks and McAfee’s model of *feints* provides one intermediate approach [19]. This model takes feints to be costly and noisy; the more a sender invests in a feint, the more likely the receiver is to observe a deceptive signal. Costly signaling allows some information to be transmitted in equilibrium. This is a similar approach to that of Kartik [23], who assigns an explicit cost to misrepresenting a type. A model of *lying* in [8] responds to [19] by arguing that signals are often cheap compared to the consequences of a receiver’s action [8]. In [8], information transmission is supported in equilibrium because some players have boundedly-rational behavioral types. The present paper follows [8] by considering costless signaling. But we explain information communication in an opposite manner. While [8] assumes that some receivers have bounded rationality, we assume that all receivers have a sort of “augmented rationality:” the ability to observe evidence of a deceptive signal.

Within literature on network security, our model is related to the *honeypot selection game with probing* studied in [24]. In this work, evidence depends on the type, but in the present work, evidence depends on both the type and the message that the sender transmits to the receiver¹. The present paper is also related to information-theoretic approaches to strategic communication, such as the one in [2]. This approach differs from our own mainly by requiring S to optimize her strategy before she observes her private information. This makes the problem a Stackelberg game rather than a signaling game.

Finally, the present work builds upon our earlier model of signaling games with evidence [32]. That work only found analytical equilibrium solutions in the degenerate cases of the model (*i.e.*, in which the detector is perfect or useless). The present work solves for all pure-strategy equilibria in the non-degenerate cases (Theorem 1). For the first time, we also solve for mixed-strategy equilibria (Theorems 2-3). In addition, our truth induction result and proof are new contributions (Theorem 4). Lastly, we present an analysis of the comparative statics of the model (Fig. 6-9), and a discussion of the robustness of the equilibrium strategies (Corollary 2). These results add significant mathematical rigor and further discussion to the model proposed in [32].

The rest of the paper proceeds as follows. Section II describes the model and equilibrium concept. In Section III, we find pure-strategy and mixed-strategy equilibria. Then Section IV evaluates the sensitivity of the equilibria to changes in detector characteristics. Section V describes the application. Finally, we discuss the implications of our results in Section VI.

II. MODEL

Signaling games are two-player games between a sender (S) and a receiver (R). These games are *information asymmetric*, because S possesses information that is unknown to R . They are also *dynamic*, because the players’ actions are not simultaneous. S transmits a message to R , and then R acts upon the message. Generally, signaling games can be *non-zero-sum*, which means that the objectives of S and R are not direct negations of each other’s objectives. Figure 1 depicts the traditional signaling game between

¹In other words, the detector in our game emits evidence when the message does not truthfully represent the type—that is, when the sender is lying.

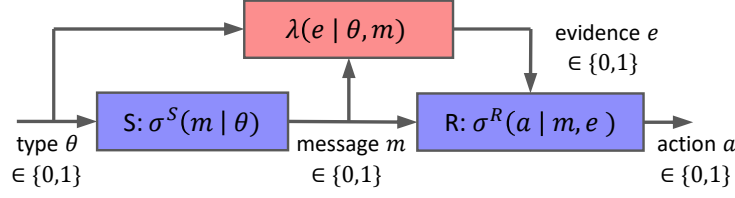


Figure 1: Signaling games with evidence add the red detector block to the S and R blocks. The probability $\lambda(e | \theta, m)$ of emitting evidence e depends on S 's type θ and the message m that she transmits.

Table I: Summary of Notation

| Notation | Meaning |
|--|--|
| S, R | Sender and Receiver |
| $\theta \in \Theta, m \in M, a \in A$ | Types, Messages, Actions |
| $u^X(\theta, m, a)$ | Utility Functions of Player $X \in \{S, R\}$ |
| $p(\theta)$ | Prior Probability of θ |
| $\sigma^S(m \theta)$ | Mixed Strategy of S of Type θ |
| $\lambda(e \theta, m)$ | Probability of e for Type θ & Message m |
| $\sigma^R(a m, e)$ | Mixed Strategy of R given m, e |
| $\mu^R(\theta m, e)$ | Belief of R that S is of Type θ |
| $\bar{u}^S(\sigma^S, \sigma^R \theta)$ | Expected Utility for S of Type θ |
| $\bar{u}^R(\sigma^R \theta, m, e)$ | Expected Utility for R given θ, m, e |
| $\alpha \in [0, 1]$ | “Size” of Detector (False Positive Rate) |
| $\beta \in [\alpha, 1]$ | “Power” of Detector (True Positive Rate) |

S and R , augmented by a detector block. We call this augmented signaling game a *signaling game with evidence*.

A. Types, Messages, Evidence, Actions, and Beliefs

We consider binary information and action spaces in order to simplify analysis. Table I summarizes the notation. Let $\theta \in \Theta = \{0, 1\}$ denote the private information of S . Signaling games refer to θ as a *type*. The type could represent, e.g., whether the sender is a malicious or benign actor, whether she has one set of preferences over another, or whether a given event observable to S but not to R has occurred. The type is drawn² from a probability distribution p , where $\sum_{\theta \in \Theta} p(\theta) = 1$ and $\forall \theta \in \Theta, p(\theta) \geq 0$.

Based on θ , S chooses a message $m \in M = \{0, 1\}$. She may use mixed strategies, i.e., she may select each m with some probability. Let $\sigma^S \in \Gamma^S$ denote the strategy of S , such that $\sigma^S(m | \theta)$ gives the probability with which S sends message m given that she is of type θ . The space of strategies satisfies

$$\Gamma^S = \left\{ \sigma^S | \forall \theta, \sum_{m \in M} \sigma^S(m | \theta) = 1; \forall \theta, m, \sigma^S(m | \theta) \geq 0 \right\}.$$

Since Θ and M are identical, a natural interpretation of an honest message is $m = \theta$, while a deceptive message is represented by $m \neq \theta$.

²Harsanyi conceptualized type selection as a randomized move by a non-strategic player called *nature* (in order to map an incomplete information game to one of complete information) [18].

Next, the detector emits evidence based on whether the message m is equal to the type θ . The detector emits $e \in E = \{0, 1\}$ with the probability³ $\lambda(e | \theta, m)$. Let $e = 1$ denote an *alarm* and $e = 0$ *no alarm*. The probability with which a detector records a true positive is called the *power* $\beta \in [0, 1]$ of the detector. For simplicity, we set both true-positive rates to be equal: $\beta = \lambda(1 | 0, 1) = \lambda(1 | 1, 0)$. Similarly, let α denote the *size* of the detector, which refers to the false-positive rate. We have $\alpha = \lambda(1 | 0, 0) = \lambda(1 | 1, 1)$. A valid detector has $\beta \geq \alpha$. This is without loss of generality, because otherwise α and β can be relabeled.

After receiving both m and e , R chooses an action $a \in A = \{0, 1\}$. R may also use mixed strategies. Let $\sigma^R \in \Gamma^R$ denote the strategy of R such that his mixed-strategy probability of playing action a given message m and evidence e is $\sigma^R(a | m, e)$. The space of strategies is $\Gamma^R =$

$$\left\{ \sigma^R \mid \forall m, e, \sum_{a \in A} \sigma^R(a | m, e) = 1; \forall e, m, a, \sigma^R(a | m, e) \geq 0 \right\}.$$

Based on m and e , R forms a belief⁴ about the type θ of S . For all θ , m , and e , define $\mu^R : \Theta \rightarrow [0, 1]$ such that $\mu^R(\theta | m, e)$ gives the likelihood with which R believes that S is of type θ given message m and evidence e . R uses belief μ^R to decide which action to choose.

B. Utility Functions

Let $u^S : \Theta \times M \times A \rightarrow \mathbb{R}$ denote a utility function for S such that $u^S(\theta, m, a)$ gives the utility that she receives when her type is θ , she sends message m , and R plays action a . Similarly, let $u^R : \Theta \times M \times A$ denote R 's utility function so that $u^R(\theta, m, a)$ gives his payoff under the same scenario.

Only a few assumptions are necessary to characterize a deceptive interaction⁵. Assumption 1 is that u^S and u^R do not depend (exogenously) on m , *i.e.*, the interaction is a cheap-talk game. Assumptions 2-3 state that R receives higher utility if he correctly chooses $a = \theta$ than if he chooses $a \neq \theta$. Formally,

$$u^R(0, m, 0) > u^R(0, m, 1), \quad u^R(1, m, 0) < u^R(1, m, 1).$$

Finally, Assumptions 4-5 state that S receives higher utility if R chooses $a \neq \theta$ than if he chooses $a = \theta$. That is,

$$u^S(0, m, 0) < u^S(0, m, 1), \quad u^S(1, m, 0) > u^S(1, m, 1).$$

Together, Assumptions 1-5 characterize a *cheap-talk signaling game with evidence*.

Define an expected utility function $\bar{u}^S : \Gamma^S \times \Gamma^R \rightarrow \mathbb{R}$ such that $\bar{u}^S(\sigma^S, \sigma^R | \theta)$ gives the expected utility to S when she plays strategy σ^S , given that she is of type θ . This expected utility is given by

$$\bar{u}^S(\sigma^S, \sigma^R | \theta) = \sum_{a \in A} \sum_{e \in E} \sum_{m \in M} \sigma^R(a | m, e) \lambda(e | \theta, m) \sigma^S(m | \theta) u^S(\theta, m, a). \quad (1)$$

³The detector can be seen as a second move by nature.

⁴The *Stanford Encyclopedia of Philosophy* lists among several definitions of deception: “to intentionally cause to have a false belief that is known and believed to be false” [26]. This suggests that belief formation is an important aspect of deception.

⁵Defining game-theoretic utility functions always involves various difficulties and approximations. In deceptive interactions, utility quantified only in financial terms may be insufficient, due to what has been called *lying aversion* [14]. Moreover, utility functions can depend highly on context. For instance, some field experiments in economics have found subjects to be less deceptive in reality than in the laboratory [11]. These objections notwithstanding, we assume some basic properties of the sender and receiver incentives that constrain the definition of the utility functions.

Note that in Eq. (1), R 's mixed-strategy probability $\sigma^R(a|m, e)$ of playing action a depends on the evidence e that he observes. S must anticipate the probability of leaking evidence e . She does this using $\lambda(e|\theta, m)$. This probability does not appear in the standard signaling-game without evidence.

Next define $\bar{u}^R : \Gamma^R \rightarrow \mathbb{R}$ such that $\bar{u}^R(\sigma^R|\theta, m, e)$ gives the expected utility to R when he plays strategy σ^R given message m , evidence e , and sender type θ . The expected utility function is given by

$$\bar{u}^R(\sigma^R|\theta, m, e) = \sum_{a \in A} \sigma^R(a|m, e) u^R(\theta, m, a).$$

C. Equilibrium Concept

In two-player games, Nash equilibrium defines a strategy profile in which each player best responds to the optimal strategy of the other player [29]. Signaling games motivate the extension of Nash equilibrium in two ways. First, information asymmetry requires R to maximize his expected utility over the possible types of S . An equilibrium in which S and R best respond to each other's strategies given some belief μ^R is called a *Bayesian Nash equilibrium* [18]. We also require R to update μ^R rationally. *Perfect Bayesian Nash equilibrium* (PBNE) captures this constraint. Definition 1 applies PBNE to signaling games with evidence.

Definition 1. (Perfect Bayesian Nash Equilibrium [13]) A PBNE of a cheap-talk signaling game with evidence is a strategy profile $(\sigma^{S*}, \sigma^{R*})$ and posterior beliefs $\mu^R(\theta|m, e)$ such that

$$\forall \theta \in \Theta, \sigma^{S*} \in \arg \max_{\sigma^S \in \Gamma^S} \bar{u}^S(\sigma^S, \sigma^{R*}|\theta), \quad (2)$$

$$\forall m \in M, \forall e \in E,$$

$$\sigma^{R*} \in \arg \max_{\sigma^R \in \Gamma^R} \sum_{\theta \in \Theta} \mu^R(\theta|m, e) \bar{u}^R(\sigma^R|\theta, m, e), \quad (3)$$

and if $\sum_{\tilde{\theta} \in \Theta} \lambda(e|\tilde{\theta}, m) \sigma^S(m|\tilde{\theta}) p(\tilde{\theta}) > 0$, then

$$\mu^R(\theta|m, e) = \frac{\lambda(e|\theta, m) \mu^R(\theta|m)}{\sum_{\tilde{\theta} \in \Theta} \lambda(e|\tilde{\theta}, m) \mu^R(\tilde{\theta}|m)}, \quad (4)$$

where

$$\mu^R(\theta|m) = \frac{\sigma^S(m|\theta) p(\theta)}{\sum_{\hat{\theta} \in \Theta} \sigma^S(m|\hat{\theta}) p(\hat{\theta})}. \quad (5)$$

If $\sum_{\tilde{\theta} \in \Theta} \lambda(e|\tilde{\theta}, m) \sigma^S(m|\tilde{\theta}) p(\tilde{\theta}) = 0$, then $\mu^R(\theta|m, e)$ may be set to any probability distribution over Θ .

Equations (4)-(5) require the belief to be set according to Bayes' Law. First, R updates her belief according to m using Eq. (5). Then R updates her belief according to e using Eq. (4). This step is not present in the traditional definition of PBNE for signaling games.

There are three categories of PBNE: *separating*, *pooling*, and *partially-separating* equilibria. These are defined based on the strategy of S . In separating PBNE, the two types of S transmit opposite messages. This allows R to infer S 's type with certainty. In pooling PBNE, both types of S send messages with

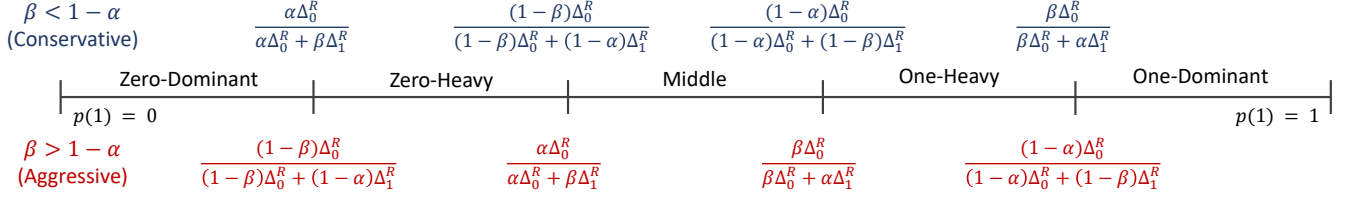


Figure 2: PBNE differ within five prior probability regimes. In the Zero-Dominant regime, $p(\theta = 1) \approx 0$, i.e., type 0 dominates. In the Zero-Heavy regime, $p(\theta = 1)$ is slightly higher, but still low. In the Middle regime, the types are mixed almost evenly. The One-Heavy regime has a higher $p(\theta = 1)$, and the One-Dominant regime has $p(\theta = 1) \approx 1$. The definitions of the regime boundaries depend on whether the detector is conservative or aggressive.

identical probabilities. That is, $\forall m \in M$, $\sigma^S(m|0) = \sigma^S(m|1)$. This makes m useless to R . R updates his belief based only on the evidence e . Equations (4)-(5) yield

$$\mu^R(\theta|m, e) = \frac{\lambda(e|\theta, m) p(\theta)}{\sum_{\tilde{\theta} \in \Theta} \lambda(e|\tilde{\theta}, m) p(\tilde{\theta})}. \quad (6)$$

In partially-separating PBNE, the two types of S transmit messages with different, but not completely opposite, probabilities. In other words, $\forall m \in M$, $\sigma^S(m|0) \neq \sigma^S(m|1)$, and $\sigma^S(m|0) \neq 1 - \sigma^S(m|1)$. Equations (4)-(5) allow R to update his belief, but the belief remains uncertain.

III. EQUILIBRIUM RESULTS

In this section, we find the PBNE of the cheap-talk signaling game with evidence. We present the analysis in four steps. In Subsection III-A, we solve the optimality condition for R , which determines the structure of the results. In Subsection III-B, we solve the optimality condition for S , which determines the equilibrium beliefs μ^R . We present the pooling equilibria of the game in Subsection III-C. Some parameter regimes do not admit any pooling equilibria. For those regimes, we derive partially-separating equilibria in Subsection III-D.

First, Lemma 1 notes that one class of equilibria is not supported.

Lemma 1. *Under Assumptions 1-5, the game admits no separating PBNE.*

Proof: See Appendix A. ■

Lemma 1 results from the opposing utility functions of S and R . S wants to deceive R , and R wants to correctly guess the type. It is not incentive-compatible for S to fully reveal the type by choosing a separating strategy.

A. Prior Probability Regimes

Next, we look for pooling PBNE. Consider R 's optimal strategies σ^{R*} in this equilibrium class. Note that if the sender uses a pooling strategy on message m (i.e., if S with both $\theta = 0$ and $\theta = 1$ send message m), then $\sigma^{R*}(1|m, e)$ gives R 's optimal action a after observing evidence e . Messages do not

Table II: $\sigma^{R*}(1|m, e)$ in Pooling PBNE

| (a) Conservative Detector: $\beta < 1 - \alpha$ | | | | | (b) Aggressive Detector: $\beta > 1 - \alpha$ | | | |
|---|-----------------------|-----------------------|-----------------------|-----------------------|---|-----------------------|-----------------------|-----------------------|
| | $\sigma^{R*}(1 0, 0)$ | $\sigma^{R*}(1 0, 1)$ | $\sigma^{R*}(1 1, 0)$ | $\sigma^{R*}(1 1, 1)$ | $\sigma^{R*}(1 0, 0)$ | $\sigma^{R*}(1 0, 1)$ | $\sigma^{R*}(1 1, 0)$ | $\sigma^{R*}(1 1, 1)$ |
| 0-D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0-H | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 |
| Middle | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 1-H | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| 1-D | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

reveal anything about the type θ , and R updates his belief using Eq. (6). For brevity, define the following notations:

$$\Delta_0^R \triangleq u^R(\theta = 0, m, a = 0) - u^R(\theta = 0, m, a = 1), \quad (7)$$

$$\Delta_1^R \triangleq u^R(\theta = 1, m, a = 1) - u^R(\theta = 1, m, a = 0). \quad (8)$$

Δ_0^R gives the benefit to R for correctly guessing the type when $\theta = 0$, and Δ_1^R gives the benefit to R for correctly guessing the type when $\theta = 1$. Since the game is a cheap-talk game, these benefits are independent of m . Lemmas 2-3 solve for σ^{R*} within five regimes of the prior probability $p(\theta)$ of each type $\theta \in \{0, 1\}$. Recall that $p(\theta)$ represents R 's belief that S has type θ before R observes m or e .

Lemma 2. For pooling PBNE, R 's optimal actions σ^{R*} for evidence e and messages m on the equilibrium path⁶ vary within five regimes of $p(\theta)$. The top half of Fig. 2 lists the boundaries of these regimes for detectors in which $\beta < 1 - \alpha$, and the bottom half of Fig. 2 lists the boundaries of these regimes for detectors in which $\beta > 1 - \alpha$.

Proof: See Appendix B. ■

Remark 1. Boundaries of the equilibrium regimes differ depending on the relationship between β and $1 - \alpha$. β is the true-positive rate and $1 - \alpha$ is the true-negative rate. Let us call detectors with $\beta < 1 - \alpha$ *conservative* detectors, detectors with $\beta > 1 - \alpha$ *aggressive* detectors, and detectors with $\beta = 1 - \alpha$ *equal-error-rate (EER)* detectors. Aggressive detectors have high true-positive rates but also high false-positive rates. Conservative detectors have low false-positive rates but also low true-positive rates. Equal-error-rate detectors have an equal rate of false-positives and false-negatives.

Remark 2. The regimes in Fig. 2 shift towards the right as Δ_0^R increases. Intuitively, a higher $p(1)$ is necessary to balance out the benefit to R for correctly identifying a type $\theta = 0$ as Δ_0^R increases. The regimes shift towards the left as Δ_1^R increases for the opposite reason.

Lemma 3 gives the optimal strategies of R in response to pooling behavior within each of the five parameter regimes.

Lemma 3. For each regime, σ^{R*} on the equilibrium path is listed in Table IIa if $\beta < 1 - \alpha$ and in Table IIb if $\beta > 1 - \alpha$. The row labels correspond to the Zero-Dominant (0-D), Zero-Heavy (0-H), Middle,

⁶In pooling PBNE, the message “on the equilibrium path” is the one that is sent by both types of S . Messages “off the equilibrium path” are never sent in equilibrium, although determining the actions that R would play if S were to transmit a message off the path is necessary in order to determine the existence of equilibria.

One-Heavy (1-H), and One-Dominant (1-D) regimes.

Proof: See Appendix B. ■

Remark 3. In the Zero-Dominant and One-Dominant regimes of all detector classes, R determines σ^{R*} based only on the overwhelming prior probability of one type over the other⁷. In the Zero-Dominant regime, R chooses $\sigma^{R*}(1|m, e) = 0$ for all m and e , and in the One-Dominant regime, R chooses $\sigma^{R*}(1|m, e) = 1$ for all m and e .

Remark 4. In the Middle regime of both detector classes, R chooses⁸ $\sigma^{R*}(1|m, 0) = m$ and $\sigma^{R*}(1|m, 1) = 1 - m$. In other words, R believes the message of S if $e = 0$ and does not believe the message of S if $e = 1$.

B. Optimality Condition for S

Next, we must check to see whether each possible pooling strategy is optimal for S . This depends on what R would do if S were to deviate and send a message off the equilibrium path. R 's action in that case depends on his beliefs for messages off the path. In PBNE, these beliefs can be set arbitrarily. The challenge is to see whether beliefs μ^R exist such that each pooling strategy is optimal for both types of S . Lemmas 4-5 give conditions under which such beliefs exist.

Lemma 4. Let m be the message on the equilibrium path. If $\sigma^{R*}(1|m, 0) = \sigma^{R*}(1|m, 1)$, then there exists a μ^R such that pooling on message m is optimal for both types of S . For brevity, let $a^* \triangleq \sigma^{R*}(1|m, 0) = \sigma^{R*}(1|m, 1)$. Then μ^R is given by,

$$\forall e \in E, \mu^R(\theta = a^* | 1 - m, e) \geq \frac{\Delta_{1-a^*}^R}{\Delta_{1-a^*}^R + \Delta_{a^*}^R}.$$

Lemma 5. If $\sigma^{R*}(1|m, 0) = 1 - \sigma^{R*}(1|m, 1)$ and $\beta \neq 1 - \alpha$, then there does not exist a μ^R such that pooling on message m is optimal for both types of S .

Proof: See Appendix C for the proofs of Lemmas 4-5. ■

The implications of these lemmas can be seen in the pooling PBNE results that are presented next.

C. Pooling PBNE

Theorem 1 gives the pooling PBNE of the game.

Theorem 1. (Pooling PBNE) The pooling PBNE are summarized by Fig. 3.

Proof: This results from combining Lemmas 2-5, which give the equilibrium σ^{S*} , σ^{R*} , and μ^R . ■

Remark 5. For $\beta < 1 - \alpha$, the Zero-Heavy regime admits only a pooling PBNE on $m = 1$, and the One-Heavy regime admits only a pooling PBNE on $m = 0$. We call this situation (in which, typically,

⁷For instance, consider an application to product reviews in an online marketplace. A product may be low ($\theta = 0$) or high ($\theta = 1$) quality. A review may describe the product as poor ($m = 0$) or as good ($m = 1$). Based on the wording of the review, R may be suspicious ($e = 1$) that the review is fake, or he may not be suspicious ($e = 0$). He can then buy ($a = 1$) or to not buy ($a = 0$) the product. According to Remark 3, if R has a strong prior belief that the product is high quality ($p(1) \approx 1$), then he will ignore both the review m and the evidence e , and he will always buy the product ($a = 1$).

⁸For the same application to online marketplaces as in Footnote 7, if R does not have a strong prior belief about the quality of the product (e.g., $p(1) \approx 0.5$), then he will trust the review (play $a = m$) if $e = 0$, and he will not trust the review (he will play $a = 1 - m$) if $e = 1$.

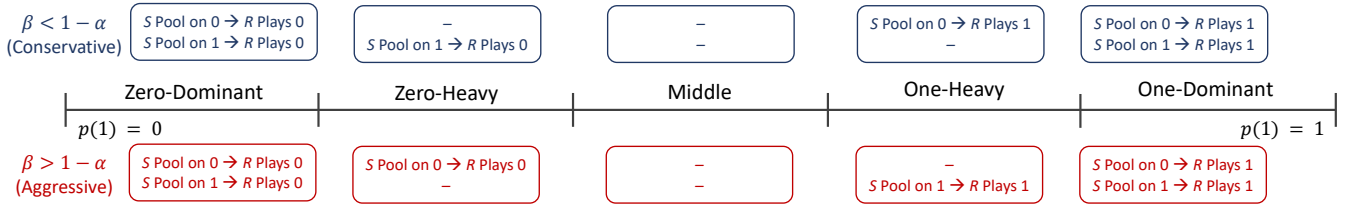


Figure 3: PBNE in each of the parameter regimes defined in Fig. 2. For $m \in \{0, 1\}$, “ S Pool on m ” signifies $\sigma^{S*}(m | 0) = \sigma^{S*}(m | 1) = 1$. For $a \in \{0, 1\}$, “ R Plays a ” signifies $\sigma^{R*}(a | 0, 0) = \sigma^{R*}(a | 0, 1) = \sigma^{R*}(a | 1, 0) = \sigma^{R*}(a | 1, 1) = 1$. Lemma 4 gives μ^R .

$m \neq \theta$) a *falsification convention*. (See Section IV.) For $\beta > 1 - \alpha$, the Zero-Heavy regime admits only a pooling PBNE on $m = 0$, and the One-Heavy regime admits only a pooling PBNE on $m = 1$. We call this situation (in which, typically, $m = \theta$) a *truth-telling convention*.

Remark 6. For $\beta \neq 1 - \alpha$, the Middle regime does not admit any pooling PBNE. This occurs because R ’s responses to message m depends on e , i.e., $\sigma^{R*}(1 | 0, 0) = 1 - \sigma^{R*}(1 | 0, 1)$ and $\sigma^{R*}(1 | 1, 0) = 1 - \sigma^{R*}(1 | 1, 1)$. One of the types of S prefers to deviate to the message off the equilibrium path. Intuitively, for a conservative detector, S with type $\theta = m$ prefers to deviate to message $1 - m$, because his deception is unlikely to be detected. On the other hand, for an aggressive detector, S with type $\theta = 1 - m$ prefers to deviate to message $1 - m$, because his honesty is likely to produce a false-positive alarm, which will lead R to guess $a = m$. Appendix C includes a formal derivation of this result.

D. Partially-Separating PBNE

For $\beta \neq 1 - \alpha$, since the Middle regime does not support pooling PBNE, we search for partially-separating PBNE. In these PBNE, S and R play mixed strategies. In mixed-strategy equilibria in general, each player chooses a mixed strategy that makes the other players indifferent between the actions that they play with positive probability. Theorems 2-3 give the results.

Theorem 2. (Partially-Separating PBNE for Conservative Detectors) For $\beta < 1 - \alpha$, within the Middle Regime, there exists an equilibrium in which the sender strategies are

$$\begin{aligned}\sigma^{S*}(m = 1 | \theta = 0) &= \frac{\beta^2}{\beta^2 - \alpha^2} - \frac{\alpha\beta\Delta_1^R}{(\beta^2 - \alpha^2)\Delta_0^R} \left(\frac{p}{1-p} \right), \\ \sigma^{S*}(m = 1 | \theta = 1) &= \frac{\alpha\beta\Delta_0^R}{(\beta^2 - \alpha^2)\Delta_1^R} \left(\frac{1-p}{p} \right) - \frac{\alpha^2}{\beta^2 - \alpha^2},\end{aligned}$$

the receiver strategies are

$$\begin{aligned}\sigma^{R*}(a = 1 | m = 0, e = 0) &= \frac{1 - \alpha - \beta}{2 - \alpha - \beta}, & \sigma^{R*}(a = 1 | m = 0, e = 1) &= 1, \\ \sigma^{R*}(a = 1 | m = 1, e = 0) &= \frac{1}{2 - a - b}, & \sigma^{R*}(a = 1 | m = 1, e = 1) &= 0,\end{aligned}$$

and the beliefs are computed by Bayes’ Law in all cases.

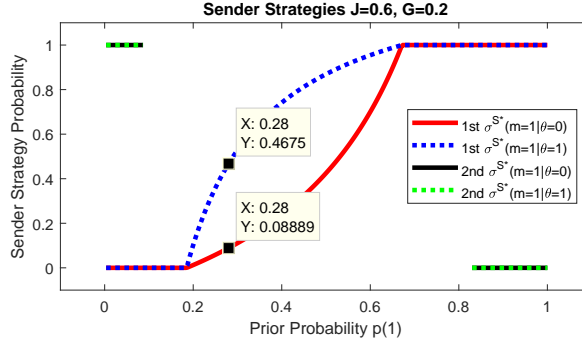


Figure 4: Equilibrium sender strategies for $\beta = 0.9$, $\alpha = 0.3$, $\Delta_0^R = 15$, and $\Delta_1^R = 22$. The Dominant regimes of $p(1)$ support both pooling on $m = 0$ and $m = 1$. The Heavy regimes ($0.09 < p < 0.19$ and $0.67 < p < 0.83$) support only pooling on $m = 0$ and $m = 1$, respectively. The Middle regime does not support any pooling PBNE, but does support a partially-separating PBNE.

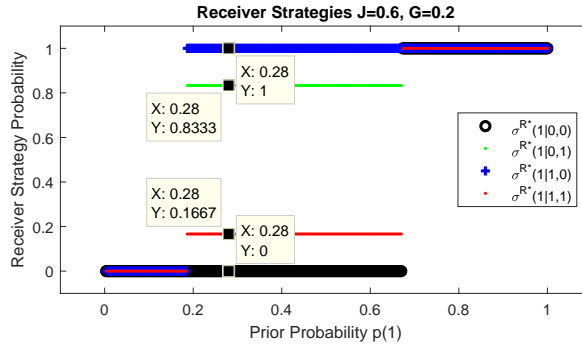


Figure 5: Equilibrium receiver strategies for $\beta = 0.9$, $\alpha = 0.3$, $\Delta_0^R = 15$, and $\Delta_1^R = 22$. R plays pure strategies in both the Dominant and Heavy regimes. In the Middle regime, two strategy components are pure, and two are mixed.

Theorem 3. (Partially-Separating PBNE for Aggressive Detectors) For any $g \in [0, 1]$, let $\bar{g} \triangleq 1 - g$. For $\beta > 1 - \alpha$, within the Middle Regime, there exists an equilibrium in which the sender strategies are

$$\sigma^{S*}(m = 1 | \theta = 0) = \frac{\bar{\alpha}\bar{\beta}\Delta_1^R}{(\bar{\alpha}^2 - \bar{\beta}^2)\Delta_0^R} \left(\frac{p}{1-p} \right) - \frac{\bar{\beta}^2}{\bar{\alpha}^2 - \bar{\beta}^2},$$

$$\sigma^{S*}(m = 1 | \theta = 1) = \frac{\bar{\alpha}^2}{\bar{\alpha}^2 - \bar{\beta}^2} - \frac{\bar{\alpha}\bar{\beta}\Delta_0^R}{(\bar{\alpha}^2 - \bar{\beta}^2)\Delta_1^R} \left(\frac{1-p}{p} \right),$$

the receiver strategies are

$$\sigma^{R*}(a = 1 | m = 0, e = 0) = 0, \quad \sigma^{R*}(a = 1 | m = 0, e = 1) = \frac{1}{\alpha + \beta},$$

$$\sigma^{R*}(a = 1 | m = 1, e = 0) = 1, \quad \sigma^{R*}(a = 1 | m = 1, e = 1) = \frac{\alpha + \beta - 1}{\alpha + \beta},$$

and the beliefs are computed by Bayes' Law in all cases.

Proof: See Appendix D for the proofs of Theorems 2-3. ■

Remark 7. In Theorem 2, S chooses the σ^{S*} that makes R indifferent between $a = 0$ and $a = 1$ when he observes the pairs $(m = 0, e = 0)$ and $(m = 1, e = 0)$. This allows R to choose mixed strategies for $\sigma^{R*}(1 | 0, 0)$ and $\sigma^{R*}(1 | 1, 0)$. Similarly, R chooses $\sigma^{R*}(1 | 0, 0)$ and $\sigma^{R*}(1 | 1, 0)$ that make both types of

S indifferent between sending $m = 0$ and $m = 1$. This allows S to choose mixed strategies. A similar pattern follows in Theorem 3 for σ^{S*} , $\sigma^{R*}(1 | 0, 1)$, and $\sigma^{R*}(1 | 1, 1)$.

Figures 4-5 depict the equilibrium strategies for S and R , respectively, for an aggressive detector. Note that the horizontal axis is the same as the horizontal axis in Fig. 2 and Fig. 3.

The Zero-Dominant and One-Dominant regimes feature two pooling equilibria. In Fig. 4, the sender strategies for the first equilibrium are depicted by the red and blue curves, and the sender strategies for the second equilibrium are depicted by the green and black curves. These are pure strategies, because they occur with probabilities of zero or one. The Zero-Heavy and One-Heavy regimes support only one pooling equilibria in each case.

The Middle regime of $p(1)$ features the partially-separating PBNE given in Theorem 3. In this regime, Fig. 5 shows that R plays a pure strategy when $e = 0$ and a mixed strategy when⁹ $e = 1$. The next section investigates the relationships between these equilibrium results and the parameters of the game.

IV. COMPARATIVE STATICS

In this section, we define quantities that we call the *quality* and *aggressiveness* of the detector. Then we define a quantity called *truth-induction*, and we examine the variation of truth-induction with the quality and aggressiveness of the detector.

A. Equilibrium Strategies versus Detector Characteristics

Consider an alternative parameterization of the detector by the pair J and G , where $J = \beta - \alpha \in [-1, 1]$, and $G = \beta - (1 - \alpha) \in [-1, 1]$. J is called *Youden's J Statistic* [41]. Since an ideal detector has high β and low α , J parameterizes the *quality* of the detector. G parameterizes the *aggressiveness* of the detector, since an aggressive detector has $\beta > 1 - \alpha$ and a conservative detector has $\beta < 1 - \alpha$. Figure 6 depicts the transformation of the axes. Note that the pair (J, G) fully specifies the pair (α, β) .

Figure 7 depicts the influences of J and G on S 's equilibrium strategy. The red (solid) curves give $\sigma^{S*}(m = 1 | \theta = 0)$, and the blue (dashed) curves represent $\sigma^{S*}(m = 1 | \theta = 1)$. Although the Zero-Dominant and One-Dominant regimes support two pooling equilibria, Fig. 7 only plots one pooling equilibrium for the sake of clarity¹⁰.

In Column 1, J is fixed and G decreases from top to bottom. The top two plots have $G > 0$, and the bottom two have $G < 0$. There is a regime change at exactly $G = 0$. At that point, the equilibrium $\sigma^{S*}(1 | 0)$ and $\sigma^{S*}(1 | 1)$ flip to their complements. Here a small perturbation in the characteristics of the detector leads to a large change in the equilibrium strategies.

Column 2 features a conservative detector: $G = -0.1$. J decreases from top to bottom. Note that a large J leads to a large Middle regime, *i.e.*, a large range of $p(1)$ for which S plays mixed strategies in equilibrium. The detector in Column 3 is aggressive: $G = 0.1$. Again, a large J leads to a large Middle regime in which S plays mixed strategies.

⁹On the other hand, for conservative detectors R plays a pure strategy when $e = 1$ and a mixed strategy when $e = 0$.

¹⁰We chose the pooling equilibrium in which $\sigma^{S*}(1 | 0)$ and $\sigma^{S*}(1 | 1)$ are continuous with the partially-separating $\sigma^{S*}(1 | 0)$ and $\sigma^{S*}(1 | 1)$ that are supported in the Middle regime.

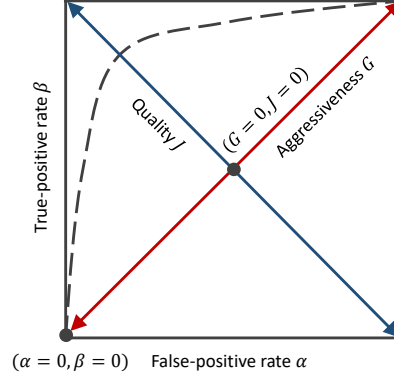


Figure 6: The detector characteristics can be plotted in ROC-space, with α on the horizontal axis and β on the vertical axis. We also parameterize the detector characteristics by the orthogonal qualities $J \in [-1, 1]$ and $G \in [-1, 1]$. The dashed line gives a sample ROC-curve.

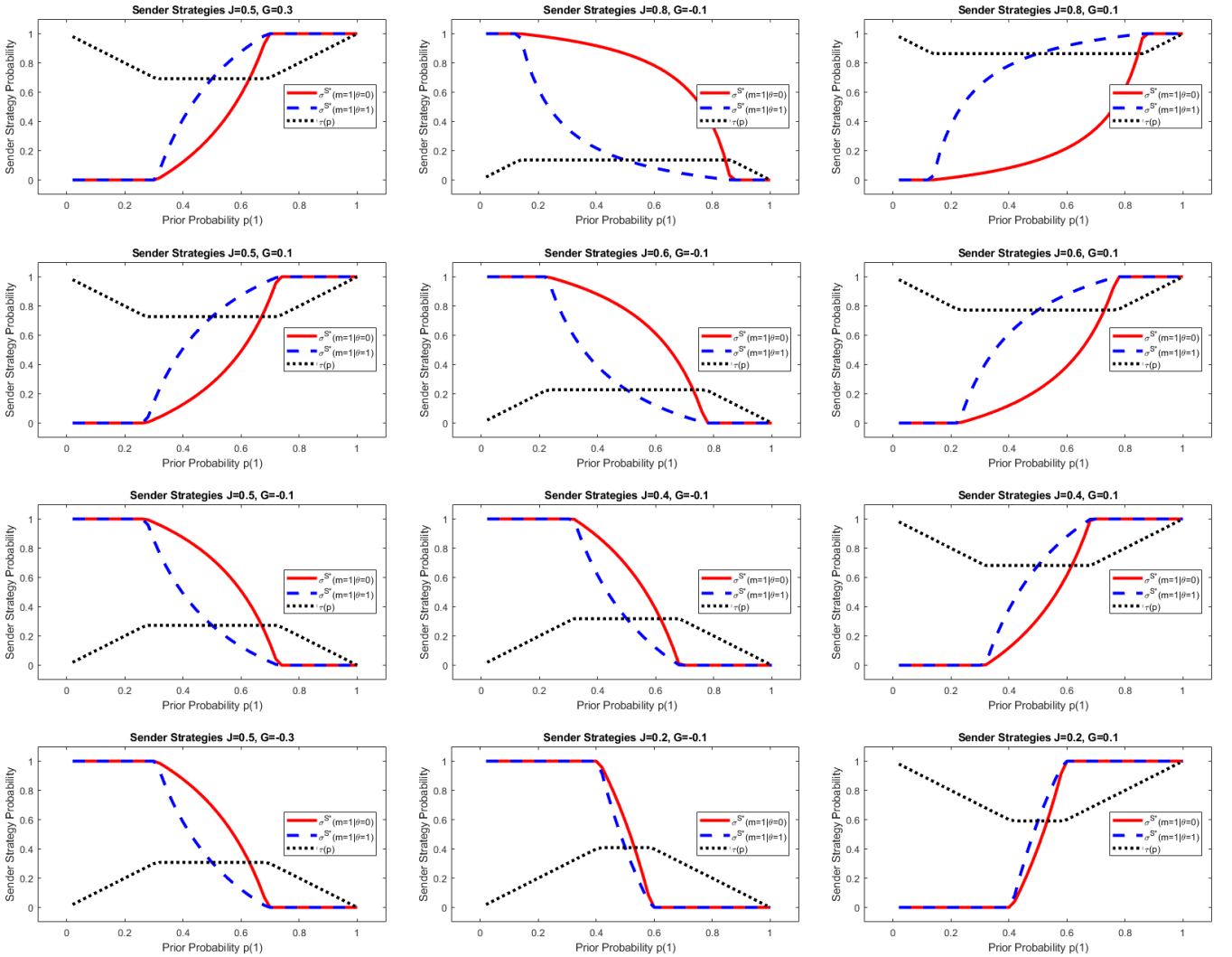


Figure 7: Sender equilibrium strategies σ^{S*} and truth-induction rates τ . Column 1: Detector quality J is fixed and aggressiveness G decreases from top to bottom. Columns 2 and 3: G is fixed and J decreases from top to bottom. Column 2 is for a conservative detector, and Column 3 is for an aggressive detector. The sender equilibrium strategies are mixed within the Middle regime and pure within the other regimes.

B. Truth-Induction

Consider the Middle regimes of the games plotted in Columns 2 and 3. Note that in the Middle regime of Column 2, the probabilities with which both types of S send $m = 1$ decrease as $p(1)$ increases, while in the Middle regime of Column 3, the probabilities with which both types of S send $m = 1$ increases as $p(1)$ increases. This suggests that S is somehow more “honest” for the aggressive detectors in Column 3, because θ and m are more correlated for aggressive detectors than for conservative detectors.

In order to formalize this result, let $\sigma^{S*}(m | \theta; p)$ parameterize the sender’s equilibrium strategy by the prior probability $p \triangleq p(1)$. Then define a mapping $\tau : [-1, 1]^2 \times [0, 1] \rightarrow [0, 1]$, such that $\tau(J, G, p)$ gives the *truth-induction rate* of the detector parameterized by (J, G) at the prior probability¹¹ p . We have

$$\tau(J, G, p) = \sum_{\theta \in \{0, 1\}} p \sigma^{S*}(m = \theta | \theta; p). \quad (9)$$

The quantity τ gives the proportion of messages sent by S for which $m = \theta$, i.e., for which S tells the truth. From this definition, we have Theorem 4.

Theorem 4. (*Detectors and Truth Induction Rates*) Set $\Delta_0^R = \Delta_1^R$. Then, within prior probability regimes that feature unique PBNE (i.e., the Zero-Heavy, Middle, and One-Heavy Regimes), for all $J \in [0, 1]$ and $\forall p \in [0, 1]$, we have that

$$\begin{aligned} \tau(J, G, p) &\leq \frac{1}{2} \text{ for } G \in (-1, 0], \\ \tau(J, G, p) &\geq \frac{1}{2} \text{ for } G \in [0, 1]. \end{aligned}$$

Proof: See Appendix E. ■

Remark 8. We can summarize Theorem 4 by stating that *aggressive detectors induce a truth-telling convention*, while *conservative detectors induce a falsification convention*.

The black, dotted curves in Fig. 7 plot $\tau(p)$ for each of the equilibrium strategies of S . In the regimes with only one pair of equilibrium strategies for S , $\tau(p) < 1/2$ in Column 2 and $\tau(p) > 1/2$ in Column 3. In the Middle regime of Column 3, $\tau(p)$ is largest for detectors with high quality J .

C. Equilibrium Utility

The *a priori* expected equilibrium utilities of S and R are the utilities that the players expect *before* θ is drawn. Denote these utilities by $\tilde{U}^S \in \mathbb{R}$ and $\tilde{U}^R \in \mathbb{R}$, respectively. For $X \in \{S, R\}$, the utilities are given by

$$\tilde{U}^X = \sum_{\theta \in \Theta} \sum_{m \in M} \sum_{e \in E} \sum_{a \in A} p(\theta) \sigma^{S*}(m | \theta) \lambda(e | \theta, m) \sigma^{R*}(a | m, e) u^X(\theta, m, a).$$

Based on numerical experiments, we offer two propositions, leaving formal proofs for future work.

Proposition 1. Fix an aggressiveness G . For all $p \in [0, 1]$, \tilde{U}^R is monotonically non-decreasing in J .

Figure 8 illustrates Proposition 1. The proposition claims that R ’s utility improves as detector quality improves. In the Middle regime of this example, R ’s expected utility increases as the quality ranges from

¹¹Feasible detectors have $J \leq 1 - |G|$. In addition, we only analyze detectors in which $\beta > \alpha$, which gives $J > 0$.

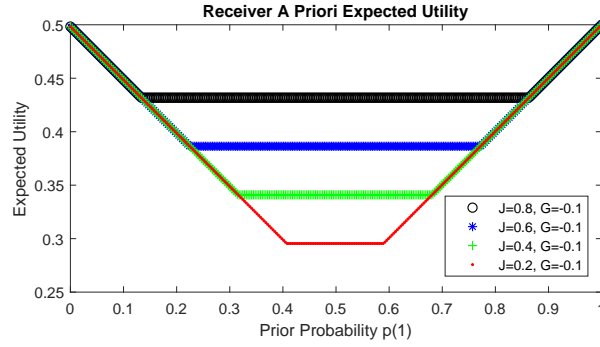


Figure 8: R 's *a priori* expected utility for varying J . Towards the extremes of $p(1)$, R 's *a priori* expected utility does not depend on J , because R ignores e . But in the middle regime, R 's expected utility increases with J .

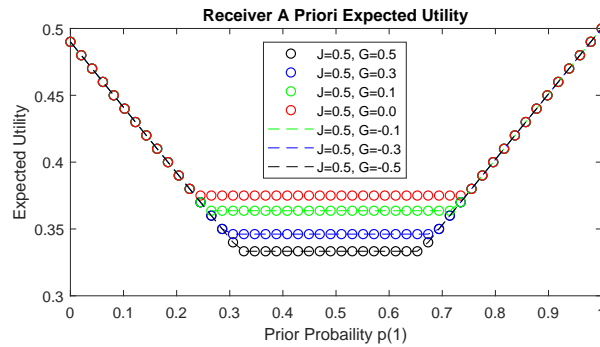


Figure 9: R 's *a priori* expected utility for varying G . Towards the extremes of $p(1)$, R 's *a priori* expected utility does not depend on G , because R ignores e . But in the middle regime, R 's expected utility decreases with $|G|$.

$J = 0.2$ to $J = 0.8$. Intuitively, as his detection ability improves, his belief μ^R becomes more certain. In the Zero-Dominant, Zero-Heavy, One-Heavy, and One-Dominant regimes, R 's equilibrium utility is not affected, because he ignores e and chooses a based only on prior probability.

Proposition 2. Fix a detector quality J . For all $p \in [0, 1]$, \tilde{U}^R is monotonically non-increasing in $|G|$.

For a fixed detector quality, Proposition 2 suggests that it is optimal for R to use an EER detector. Figure 9 plots R 's expected *a priori* equilibrium utility for various G given a fixed value of J . In the example, the same color is used for each detector with aggressiveness G and its opposite $-G$. Detectors with $G \geq 0$ are plotted using circles, and detectors with $G < 0$ are plotted using dashed lines. The utilities are the same for detectors with G and $-G$. In the Middle regime, expected utility increases as $|G|$ decreases from 0.5 to 0.

V. CASE STUDY

In this section, we apply signaling games with evidence to the use of defensive deception for network security. We illustrate the physical meanings of the action sets and equilibrium outcomes of the game for this application. We also present several results based on numerical experiments.

A. Motivation

Traditional cybersecurity technologies such as firewalls, cryptography, and role-based access control (RBAC) are insufficient against new generations of sophisticated and well-resourced adversaries. Attackers capable of *advanced persistent threats (APTs)* use techniques such as social engineering and hardware exploits to circumvent defenses and gain insider access. Stealthy and evasive maneuvers are crucial elements of APTs. Often, attackers are able to remain within a network for several months or years before they are detected by network defenders [6]. This gives the attackers an advantage of information asymmetry.

To counteract this information asymmetry, defenders have developed various technologies that detect attackers and provide attackers with false information. In fact, *honeypots* are classical mechanisms that achieve both goals. Honeypots are systems placed within a network in such a manner that the systems are never accessed by legitimate users. Any activity on the honeypots is evidence that the network has been breached by an attacker. Sophisticated honeypots emulate multiple services in order to appear legitimate. This is a form of defensive deception. At the same time, attackers may be able to detect that a deceptive program is running [10].

B. Signaling and Detection

Honeypots can roughly be divided into low-, medium-, and high-interaction, depending on the degree to which they simulate real systems. Low- and medium-interaction honeypots collect initial data about an attacker, but do not support sustained attacker activity. High-interaction honeypots provide a longer duration of deception [39].

Low- and medium-interaction honeypots often use virtual machines in order to run multiple instances on the same hardware. This causes detectable performance degradation [12]. High-interaction honeypots emulate more services than low- and medium-interaction honeypots, but this also presents more opportunities for leaking evidence of deception. Such evidence may include irregular hardware components, uncharacteristic behavior, or hints of monitoring software [20].

Without the use of deceptive technologies, attackers expect that nodes that are highly active (*e.g.*, that provide many services, allow outgoing traffic, and show recent user activity) are production systems, while nodes that are less active may be honeypots. Of course, network administrators can use programs to simulate high activity levels on honeypots. This is a type of deceptive signaling. Interestingly, some research has also suggested artificially making normal systems appear to be honeypots, as a method of deterring attackers [37]. This is an opposite form of deceptive signaling. Both of these modifications leave traces that attackers may be able to detect.

C. Model Description

1) *Players and Types*: Figure 10 casts the honeypot interaction as a signaling game with evidence. The players are the *network defender* (the sender, S) and the *attacker* (the receiver, R). The private information of the sender is the type of the system, $\theta \in \{0, 1\}$, where $\theta = 0$ represents a *production system*, and $\theta = 1$ represents a *honeypot*.

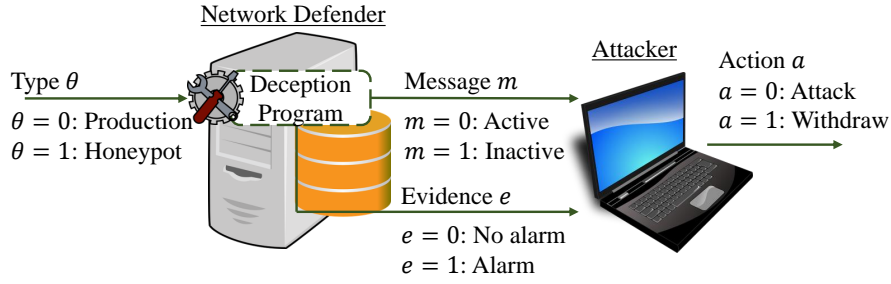


Figure 10: A defender adds either a production system or a honeypot to a network. Without any deception, the activity level of the system is $m = \theta$. The defender can run a deception program in order to set $m = 1 - \theta$, but the attacker can detect this program ($e = 1$) with some probability. Then the attacker decides whether to attack.

2) *Messages*: Typically, production systems have high activity, and honeypots have low activity. Let $m = 0$ denote that the system is *active*, and let $m = 1$ denote that the system is *inactive*. In order to deceive R , S can manipulate the activity level of the system. For instance, with a honeypot, S can send packets from some other source to the honeypot, create a program to simulate mouse movement on the honeypot, and create icons on the desktop. All of these make the honeypot appear active: $m = 0$. Similarly, with a production system, S can write programs or create user policies that decrease incoming traffic or limit mouse movement and the number of visible desktop icons. All of these make the production system appear to be inactive: $m = 1$.

3) *Evidence*: With some probability, R can detect the use of programs that manipulate the activity level of the system. For instance, if S makes a honeypot ($\theta = 1$) appear active ($m = 0$), R may observe that incoming traffic comes from a single automated source rather than from multiple human sources. He may also observe that simulated mouse movement follows patterns different from normal mouse movement, or that desktop icons are never used. These constitute an *alarm*: $e = 1$. If R does not notice these suspicious signals, then there is *no alarm*: $e = 0$. Similarly, if S creates programs or user policies for a production system ($\theta = 0$) that limit the incoming traffic and user activity ($m = 1$), R may observe evidence that user behaviors are being artificially manipulated, which constitutes an alarm: $e = 1$. If R does not notice this manipulation, then there is no alarm: $e = 0$.

4) *Actions*: After observing the activity level m and leaked evidence e , R chooses an action $a \in \{0, 1\}$. Let $a = 0$ denote *attack*, and let $a = 1$ denote *withdraw*. Notice that R prefers to choose $a = \theta$, while S prefers that R choose $a \neq \theta$. Hence, Assumptions 2-5 are satisfied. If the cost of running the deceptive program is negligible, then Assumption 1 is also satisfied.

D. Equilibrium Results

We set the utility functions according to [5], [32]. Consider a detector with a true-positive rate $\beta = 0.9$ and a false-positive rate $\alpha = 0.3$. This detector has $\beta > 1 - \alpha$, so it is an aggressive detector, and the boundaries of the equilibrium regimes are given in the bottom half of Fig. 2. For this application, the Zero-Dominant and Zero-Heavy regimes can be called the Production-Dominant and Production-Heavy regimes, since type $\theta = 0$ represents a production system. Similarly, the One-Heavy and One-Dominant regimes can be called the Honeytrap-Heavy and Honeytrap-Dominant regimes.

We have plotted the equilibrium strategies for these parameters in Fig. 4-5 in Section III. In the Production-Dominant regime ($p(\theta = 1) < 0.09$), there are very few honeypots. In equilibrium, S can set both types of systems to a high activity level ($m = 0$) or set both types of systems to a low activity level ($m = 1$). In both cases, regardless of the evidence e , R attacks. Next, for the Production-Heavy regime ($0.09 < p(1) < 0.19$), the only equilibrium strategy for S is a pooling strategy in which she leaves production systems ($\theta = 0$) active ($m = 0$) and runs a program on honeypots ($\theta = 1$) in order to make them appear active ($m = 1$) as well. R is able to detect ($e = 1$) the deceptive program on honeypots with probability $\beta = 0.9$, yet the prior probability $p(1)$ is low enough that it is optimal for R to ignore the evidence and attack ($a = 1$).

The Middle regime covers prior probabilities $0.19 < p(1) < 0.67$. The figures display the players' mixed strategies at $p(1) = 0.28$. For honeypots, S 's optimal strategy is to leave the activity level low with approximately 50% probability ($\sigma^{S*}(1|1) \approx 0.47$) and to simulate a high activity level with approximately 50% probability. For production systems, S 's optimal strategy is to decrease the activity level with a low probability ($\sigma^{S*}(1|0) \approx 0.09$) and to leave the activity level high with the remaining probability.

In the Middle regime, the receiver plays according to the activity level—*i.e.*, trusts S 's message—if $e = 0$. If $e = 1$ when $m = 0$, then most of the time, R does not trust S ($\sigma^{R*}(1|0, 1) \approx 0.83$). Similarly, if $e = 1$ when $m = 1$, then most of the time, R does not trust S ($\sigma^{R*}(1|1, 1) \approx 0.17$). The pattern of equilibria in the Honeypot-Heavy and Honeypot-Dominant regimes is similar to the pattern of equilibria in the Production-Heavy and Production-Dominant regimes.

E. Numerical Experiments and Insights

1) *Equilibrium Utility of the Sender:* Next, Corollary 1 considers the relationship between S 's *a priori* equilibrium utility and the quality J of the detector.

Corollary 1. *Fix an aggressiveness G and prior probability $p(1)$. S 's *a priori* expected utility \tilde{U}^S is not necessarily a decreasing function of the detector quality J .*

Proof: Figure 11 provides a counter-example. ■

Corollary 1 is counter-intuitive, because it seems that the player who attempts deception (S) should prefer poor deception detectors. Surprisingly, this is not always the case. Figure 11 displays the equilibrium utility for S in the honeypot example for three different J . At $p(1) = 0.4$, S receives the highest expected utility for the lowest quality deception detector. But at $p(1) = 0.1$, S receives the highest expected utility for the highest quality deception detector. In general, this is possible because the equilibrium regimes and strategies (*e.g.*, in Theorems 1-3) depend on the utility parameters of R , not S .

In particular, this occurs because of an asymmetry between the types. S does very poorly if for a production system ($\theta = 0$), she fails to deceive R , so R attacks ($a = 0$). On the other hand, S does not do very poorly if for a honeypot ($\theta = 1$), she fails to deceive R , who simply withdraws¹² ($a = 1$).

¹²For example, consider $p = 0.1$. If R has access to a low-quality detector, then $p = 0.1$ is within the Zero-Heavy regime. Therefore, R ignores e and always chooses $a = 0$. This is a “reckless” strategy that is highly damaging to S . On the other hand, if R has access to a high-quality detector, then $p = 0.1$ is within the Middle regime. In that case, R chooses a based on e . This “less reckless” strategy actually improves S 's expected utility, because R chooses $a = 0$ less often.

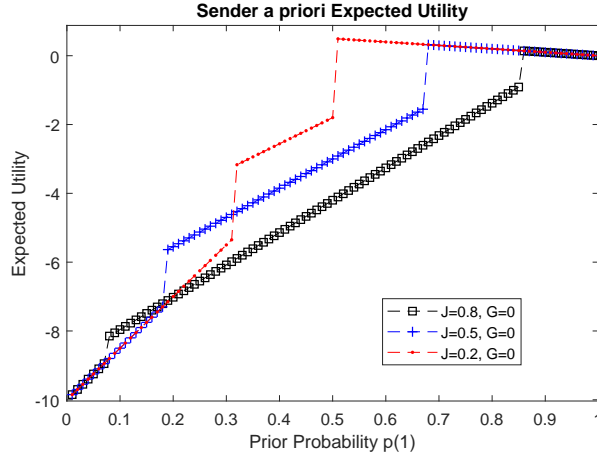


Figure 11: S 's *a priori* expected utility for varying J . From least accurate detector to most accurate detector, the curves are colored red, blue, and black. Suprisingly, for some p , S does better with more accurate detectors than with less accurate detectors.

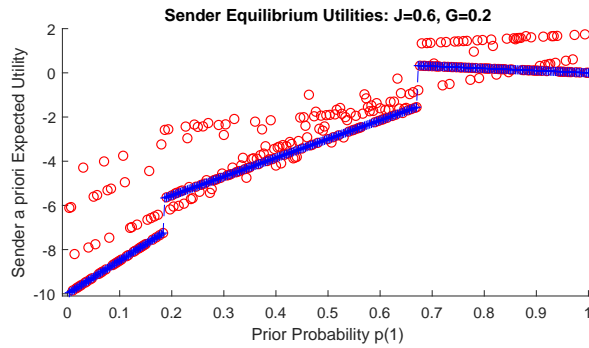


Figure 12: S 's *a priori* expected utility for playing her equilibrium strategy against 1) R 's equilibrium strategy (in blue crosses), and 2) sub-optimal strategies of R (in red circles). Deviations from R 's equilibrium strategy almost always increase the expected utility of S .

2) *Robustness of the Equilibrium Strategies*: Finally, we investigate the performance of these strategies against sub-optimal strategies of the other player. Figure 12 shows the expected utility for S when R acts optimally in blue, and the expected utility for S when R occasionally acts sub-optimally in red. In almost all cases, S earns higher expected utility if R plays sub-optimally than if R plays optimally.

It can also be shown that R 's strategy is robust against a sub-optimal S . In fact, R 's equilibrium utility remains exactly the same if S plays sub-optimally.

Corollary 2. *The a priori expected utility of R for a fixed σ^{R*} does not vary with σ^S . That is, for all $\sigma^S \in \Gamma^S$, \tilde{U}^R satisfies*

$$\begin{aligned} \sum_{\theta \in \Theta} \sum_{m \in M} \sum_{e \in E} \sum_{a \in A} p(\theta) \sigma^{S*}(m | \theta) \lambda(e | \theta, m) \sigma^{R*}(a | m, e) u^R(\theta, m, a) \\ = \sum_{\theta \in \Theta} \sum_{m \in M} \sum_{e \in E} \sum_{a \in A} p(\theta) \sigma^S(m | \theta) \lambda(e | \theta, m) \sigma^{R*}(a | m, e) u^R(\theta, m, a). \end{aligned}$$

Proof: See Appendix F. ■

Corollary 2 states that R 's equilibrium utility is not affected at all by deviations in the strategy of S .

This is a result of the structure of the partially-separating equilibrium. It suggests that R 's equilibrium strategy performs well even if S is not fully rational.

VI. DISCUSSION

We have analyzed a holistic and quantitative model of detectable deception called signaling games with evidence. The detector mechanism can be conceptualized in two ways. It can be seen as a technology that the receiver uses to detect deception. For instance, technology for a GPS receiver can detect spoofed position data based on a lack of variance in the carrier phase of the signal [36]. Alternatively, the detector can be seen as the inherent tendency of the information sender to emit cues during deceptive behavior. One example of this can be found in deceptive opinion spam in online marketplaces; fake reviews in these marketplaces tend to lack sensorial and concrete language such as spatial information [30]. Of course, both viewpoints are complementary, because cues of deceptive behavior are necessary in order for technology to be able to detect deception.

Our equilibrium results include a regime in which the receiver should choose whether to trust the sender based on the detector evidence (*i.e.*, the Middle regime), and regimes in which the receiver should ignore the message and evidence and guess the private information using only the prior probabilities (the Zero-Dominant, Zero-Heavy, One-Heavy, and One-Dominant regimes). For the sender, our results indicate that it is optimal to partially reveal the private information in the former regime, while pooling behavior is optimal in the latter regimes. The analytical bounds that we have obtained on these regimes can be used to implement policies online, since they do not require iterative numerical computation.

We have also presented several contributions that are relevant for mechanism design. For instance, the mechanism designer can maximize the receiver utility by choosing an EER detector. Practically, designing the detector involves setting a threshold within a continuous space in order to classify an observation as an “Alarm” or “No Alarm.” For an EER detector, the designer chooses a threshold that obtains equal false-positive and false-negative error rates.

At the same time, we have shown that aggressive detectors induce a truth-telling convention, while conservative detectors of the same quality induce a falsification convention. This is important if truthful communication is considered to be a design objective in itself. One area in which this applies is trust management. In both human and autonomous behavior, an agent is trustworthy if it is open and honest, if “its capabilities and limitations [are] made clear; its style and content of interactions [do] not misleadingly suggest that it is competent where it is really not” [22]. Well-designed detectors can incentivize such truthful revelation of private information.

Additionally, even deceivers occasionally prefer to reveal some true information. Our numerical results have shown that the deceiver (the sender) sometimes receives a higher utility for a high quality detector than for a low quality detector. This result suggests that cybersecurity techniques that use defensive deception should not always strive to eliminate leakage. Sometimes, revealing cues to deception serves as a deterrent. Finally, the strategies of the sender and receiver are robust to non-equilibrium actions by the other player. This emerges from the strong misalignment between their objectives.

Future work could focus on the application of signaling games with evidence to specific technical domains. These domains often require adaptations of the model. For instance, problems with continuous

type and message spaces can be addressed by applying a filter that maps the types and messages into binary spaces (*c.f.*, Section VI of [35]). Computational methods can be used to address large, discrete action spaces. In other work, we have considered signaling games with evidence in which receivers have heterogeneous abilities to detect deception [34]. Signaling games with evidence can also be embedded within larger frameworks in order to study deception in cyber-physical systems or deception across multiple links in a network. The present work provides theoretical foundations and fundamental insights that serve as a foundation for these further developments.

APPENDIX A

ELIMINATION OF SEPARATING PBNE

Two separating PBNE are possible. In the first both types are honest: $\sigma^S(0|0) = \sigma^S(1|1) = 1$. Then R believes they are telling the truth with certainty, regardless of the detector evidence. R trusts S and plays $a = m$. But both types of S would prefer to induce the action that the other type induces. Therefore, they deviate from the above strategies, and truth-telling is not an equilibrium.

The other type of separating PBNE is for both types of S to try to deceive R . Then R believes with certainty that they are both lying: $\mu^R(0|1, e) = 1$ and $\mu^R(1|0, e) = 1$. She plays $a \neq m$. Again, both types of S would prefer the a that the other type induces. Therefore, each type of S switches to the strategy of the other type, and complete dishonesty is not an equilibrium. In summary, no separating PBNE exist.

APPENDIX B

OPTIMAL ACTIONS OF R IN POOLING PBNE

Consider the case in which both types of S send $m = 0$. On the equilibrium path, Eq. (6) yields

$$\mu^R(0|0, 0) = \frac{(1 - \alpha)p(0)}{(1 - \alpha)p(0) + (1 - \beta)p(1)},$$

$$\mu^R(0|0, 1) = \frac{\alpha p(0)}{\alpha p(0) + \beta p(1)},$$

while off the equilibrium path, the beliefs can be set arbitrarily. From Eq. (3), R chooses action $a = 0$ (*e.g.*, R believes the signal of S) when evidence $e = 0$ and

$$p(0) \geq \frac{\Delta_1^R(1 - \beta)}{\Delta_0^R(1 - \alpha) + \Delta_1^R(1 - \beta)},$$

or when evidence $e = 1$ and

$$p(0) \geq \frac{\Delta_1^R\beta}{\Delta_0^R\alpha + \Delta_1^R\beta}.$$

Next, consider the case in which both types of S send $m = 1$. Equation (6) yields

$$\mu^R(0|1, 0) = \frac{(1 - \beta)p(0)}{(1 - \beta)p(0) + (1 - \alpha)p(1)},$$

$$\mu^R(0|1, 1) = \frac{\beta p(0)}{\beta p(0) + \alpha p(1)},$$

which leads R to choose action $a = 1$ (e.g. to believe the signal of S) if $e = 0$ and

$$p(0) \leq \frac{\Delta_1^R (1 - \alpha)}{\Delta_0^R (1 - \beta) + \Delta_1^R (1 - \alpha)},$$

or if $e = 1$ and

$$p(0) \leq \frac{\Delta_1^R \alpha}{\Delta_0^R \beta + \Delta_1^R \alpha}.$$

The order of these probabilities depends on whether $\beta > 1 - \alpha$.

APPENDIX C

OPTIMAL ACTIONS OF S IN POOLING PBNE

Let S pool on a message m . Consider the case that $\sigma^{R*}(1|m, 0) = \sigma^{R*}(1|m, 1)$, and let $a^* \triangleq \sigma^{R*}(1|m, 0) = \sigma^{R*}(1|m, 1)$. Then S of type $\theta = 1 - a^*$ always successfully deceives R . Clearly, that type of S does not have an incentive to deviate. But type S of type $\theta = a^*$ never deceives R . We must set the off-equilibrium beliefs such that S of type $\theta = a^*$ also would not deceive R if she were to deviate to the other message. This is the case if $\forall e \in E$,

$$\forall e \in E, \mu^R(a^* | 1 - m, e) \geq \frac{\Delta_{1-a^*}^R}{\Delta_{1-a^*}^R + \Delta_{a^*}^R}.$$

In that case, both types of S meet their optimality conditions, and we have a pooling PBNE.

But consider the case if $\sigma^{R*}(1|m, 0) = 1 - \sigma^{R*}(1|m, 1)$, (i.e., if R 's response depends on evidence e). On the equilibrium path, S of type m receives utility

$$u^S(m, m, m)(1 - \alpha) + u^S(m, m, 1 - m)\alpha, \quad (10)$$

and S of type $1 - m$ receives utility

$$u^S(1 - m, m, 1 - m)\beta + u^S(1 - m, m, m)(1 - \beta). \quad (11)$$

Now we consider R 's possible response to messages *off* the equilibrium path.

First, there cannot be a PBNE if R were to play the same action with both $e = 0$ and $e = 1$ off the equilibrium path. In that case, one of the S types could guarantee deception by deviating to message $1 - m$. Second, there cannot be a PBNE if R were to play action $a = m$ in response to message $1 - m$ with evidence 0 but action $a = 1 - m$ in response to message $1 - m$ with evidence 1. It can be shown that both types of S would deviate. The third possibility is that R plays action $a = 1 - m$ in response to message $1 - m$ if $e = 0$ but action $a = m$ in response to message $1 - m$ if $e = 1$. In that case, for deviating to message $1 - m$, S of type m would receive utility

$$u^S(m, 1 - m, m)\beta + u^S(m, 1 - m, 1 - m)(1 - \beta), \quad (12)$$

and S of type $1 - m$ would receive utility

$$u^S(1 - m, 1 - m, 1 - m)(1 - \alpha) + u^S(1 - m, 1 - m, m)\alpha. \quad (13)$$

Combining Eq. (10-12), S of type m has an incentive to deviate if $\beta < 1 - \alpha$. On the other hand, combining Eq. (11-13), S of type $1 - m$ has an incentive to deviate if $\beta > 1 - \alpha$. Therefore, if $\beta \neq 1 - \alpha$, one type of S always has an incentive to deviate, and a pooling PBNE is not supported.

APPENDIX D

DERIVATION OF PARTIALLY-SEPARATING EQUILIBRIA

For brevity, define the notation $q \triangleq \sigma^{S^*}(1|0)$, $r \triangleq \sigma^{S^*}(1|1)$, $w \triangleq \sigma^{R^*}(1|0,0)$, $x \triangleq \sigma^{R^*}(1|0,1)$, $y \triangleq \sigma^{R^*}(1|1,0)$, $z \triangleq \sigma^{R^*}(1|1,1)$, and $K \triangleq \Delta_1^R/(\Delta_0^R + \Delta_1^R)$.

We prove Theorem 2. First, assume the receiver's pure strategies $x = 1$ and $z = 0$. Second, R must choose w and y to make both types of S indifferent. This requires

$$\begin{bmatrix} \bar{\alpha} & -\bar{\beta} \\ \bar{\beta} & -\bar{\alpha} \end{bmatrix} \begin{bmatrix} w \\ y \end{bmatrix} = \begin{bmatrix} -\alpha \\ -\beta \end{bmatrix},$$

where $w, y \in [0, 1]$. Valid solutions require $\beta \leq 1 - \alpha$.

Third, S must choose q and r to make R indifferent for $(m, e) = (0, 0)$ and $(m, e) = (1, 0)$, which are the pairs that pertain to the strategies w and y . S must satisfy

$$\begin{bmatrix} -\bar{\alpha}\bar{p}\bar{K} & \bar{\beta}pK \\ -\bar{\beta}\bar{p}\bar{K} & \bar{\alpha}pK \end{bmatrix} \begin{bmatrix} q \\ r \end{bmatrix} = \begin{bmatrix} -\bar{\alpha}\bar{p}\bar{K} + \bar{\beta}pK \\ 0 \end{bmatrix}.$$

Valid solutions require p to be within the Middle regime for $\beta \leq 1 - \alpha$.

Fourth, we must verify that the pure strategies $x = 1$ and $z = 0$ are optimal. This requires

$$\frac{\alpha\bar{r}p}{\alpha\bar{r}p + \beta\bar{q}\bar{p}} \leq \bar{K} \leq \frac{\beta rp}{\beta rp + \alpha q\bar{p}}.$$

It can be shown that, after substitution for q and r , this always holds. Fifth, the beliefs must be set everywhere according to Bayes' Law. We have proved Theorem 2.

Now we prove Theorem 3. First, assume the receiver's pure strategies $w = 0$ and $y = 1$. Second, R must choose x and z to make both types of S indifferent. This requires

$$\begin{bmatrix} \alpha & -\beta \\ \beta & -\alpha \end{bmatrix} \begin{bmatrix} x \\ z \end{bmatrix} = \begin{bmatrix} \bar{\beta} \\ \bar{\alpha} \end{bmatrix},$$

where $x, z \in [0, 1]$. Valid solutions require $\beta \geq 1 - \alpha$.

Third, S must choose q and r to make R indifferent for $(m, e) = (0, 1)$ and $(m, e) = (1, 1)$, which are the pairs that pertain to the strategies x and z . S must satisfy

$$\begin{bmatrix} -\alpha\bar{p}\bar{K} & \beta pK \\ -\beta\bar{p}\bar{K} & \alpha pK \end{bmatrix} \begin{bmatrix} q \\ r \end{bmatrix} = \begin{bmatrix} -\alpha\bar{p}\bar{K} + \beta pK \\ 0 \end{bmatrix}.$$

Valid solutions require p to be within the Middle regime for $\beta \geq 1 - \alpha$.

Fourth, we must verify that the pure strategies $w = 0$ and $y = 1$ are optimal. This requires

$$\frac{\alpha\bar{r}p}{\alpha\bar{r}p + \beta\bar{q}\bar{p}} \leq \bar{K} \leq \frac{\beta rp}{\beta rp + \alpha q\bar{p}}.$$

It can be shown that, after substitution for q and r , this always holds. Fifth, the beliefs must be set everywhere according to Bayes' Law. We have proved Theorem 3.

APPENDIX E TRUTH-INDUCTION PROOF

We prove the theorem in two steps: first for the Middle regime and second for the Zero-Heavy and One-Heavy regimes.

For conservative detectors in the Middle regime, substituting the equations of Theorem 2 into Eq. (9) gives

$$\tau(J, G, p) = \frac{\bar{\alpha}\bar{\beta} - \bar{\beta}^2}{\bar{\alpha}^2 - \bar{\beta}^2} = \frac{1}{2} \left(1 - \frac{J}{1 - G} \right) \leq \frac{1}{2}.$$

For aggressive detectors in the Middle regime, substituting the equations of Theorem 3 into Eq. (9) gives

$$\tau(J, G, p) = \frac{\beta^2 - \alpha\beta}{\beta^2 - \alpha^2} = \frac{1}{2} \left(1 + \frac{J}{1 + G} \right) \geq \frac{1}{2}.$$

This proves the theorem for the Middle regime.

Now we prove the theorem for the Zero-Heavy and One-Heavy regimes. Since $\Delta_0^R = \Delta_1^R$, all of the Zero-Heavy regime has $p(1) \leq 1/2$, and all of the One-Heavy regime has $p(1) \geq 1/2$. For conservative detectors in the Zero-Heavy regime, both types of S transmit $m = 1$. S of type $\theta = 0$ are lying, while type $\theta = 1$ are telling the truth. Since $p(1) \leq 1/2$, we have $\tau \leq 1/2$. Similarly, in the One-Heavy regime, both types of S transmit $m = 0$. S of type $\theta = 0$ are telling the truth, while S of type $\theta = 1$ are lying. Since $p(1) \geq 1/2$, we have $\tau \leq 1/2$. On the other hand, for aggressive detectors, both types of S transmit $m = 0$ in the Zero-Heavy regime and $m = 1$ in the One-Heavy regime. This yields $\tau \geq 1/2$ in both cases. This proves the theorem for the Zero-Heavy and One-Heavy regimes.

APPENDIX F ROBUSTNESS PROOF

Corollary 2 is obvious in the pooling regimes. In those regimes, $\sigma^{R*}(1 | m, e)$ has the same value for all $m \in M$ and $e \in E$ (c.f., Tables IIa-IIb), so if S plays the message off the equilibrium path, then there is no change in R 's action. In the mixed strategy regimes, using the expressions for σ^{R*} from Theorems 2-3, it can be shown that, $\forall \theta \in \Theta, m \in M, a \in A$,

$$\sum_{e \in E} \lambda(e | \theta, m) \sigma^{R*}(a | m, 0) = \sum_{e \in E} \lambda(e | \theta, 1 - m) \sigma^{R*}(a | 1 - m, 0).$$

In other words, for both types of S , choosing both messages results in the same probability distribution over R 's actions. Since u^R does not depend on m , both messages result in the same utility for R .

REFERENCES

- [1] Internet security threat report. Technical report, Symantec, 2016.
- [2] Emrah Akyol, Cédric Langbort, and Tamer Başar. Information-theoretic approach to strategic communication as a hierarchical game. *Proc. of the IEEE*, 105(2):205–218, 2017.
- [3] Luigi Atzori, Antonio Iera, and Giacomo Morabito. The Internet of things: A survey. *Comput. Networks*, 54(15):2787–2805, 2010.

- [4] Rudolf Avenhaus, Bernhard Von Stengel, and Shmuel Zamir. Inspection games. *Handbook of Game Theory with Econ. Applications*, 3:1947–1987, 2002.
- [5] Thomas E Carroll and Daniel Grosu. A game theoretic investigation of deception in network security. *Security and Commun. Nets.*, 4(10):1162–1172, 2011.
- [6] Ping Chen, Lieven Desmet, and Christophe Huygens. A study on advanced persistent threats. In *IFIP Intl. Conf. on Communications and Multimedia Security*, pages 63–72. Springer, 2014.
- [7] Hugh Cott. *Adaptive Coloration in Animals*. Methuen, 1940.
- [8] Vincent P Crawford. Lying for strategic advantage: Rational and boundedly rational misrepresentation of intentions. *American Econ. Rev.*, 93(1):133–149, 2003.
- [9] Vincent P Crawford and Joel Sobel. Strategic information transmission. *Econometrica: J. of the Econometric Soc.*, pages 1431–1451, 1982.
- [10] Maximillian Dornseif, Thorsten Holz, and Christian N Klein. Nosebreak-attacking honeynets. In *Proc. IEEE SMC Inform. Assurance Workshop*, pages 123–129. IEEE, 2004.
- [11] Urs Fischbacher and Franziska Föllmi-Heusi. Lies in disguise—an experimental study on cheating. *J. of the European Econ. Assoc.*, 11(3):525–547, 2013.
- [12] Xinwen Fu, Wei Yu, Dan Cheng, Xuejun Tan, Kevin Streff, and Steve Graham. On recognizing virtual honeypots and countermeasures. In *IEEE Intl. Symp. Dependable, Autonomic and Secure Computing*, pages 211–218, 2006.
- [13] Drew Fudenberg and Jean Tirole. *Game Theory*. The MIT Press, 1991.
- [14] Uri Gneezy. Deception: The role of consequences. *American Econ. Review*, 95(1):384–394, 2005.
- [15] Sanford J Grossman. The informational role of warranties and private disclosure about product quality. *J. of Law and Econ.*, 24(3):461–483, 1981.
- [16] Sanford J Grossman and Oliver D Hart. Disclosure laws and takeover bids. *J. of Finance*, 35(2):323–334, 1980.
- [17] Erika Harrell. Victims of identity theft, 2014. *US Dept. of Justice Bureau of Justice Stat. Bulletin*, September 2015.
- [18] John C Harsanyi. Games with incomplete information played by “Bayesian” players. *Manage. Sci.*, 50(12):1804–1817, 1967.
- [19] Kenneth Hendricks and R Preston McAfee. Feints. *J of Econ. & Management Strategy*, 15(2):431–456, 2006.
- [20] Thorsten Holz and Frederic Raynal. Detecting honeypots and other suspicious environments. In *Proc. IEEE SMC Inform. Assurance Workshop*, pages 29–36, 2005.
- [21] Lech J. Janczewski and Andrew M. Colarik. *Cyber Warfare and Cyber Terrorism*. Inform. Sci. Reference, New York, 2008.
- [22] Patricia M Jones and Christine M Mitchell. Human-computer cooperative problem solving: Theory, design, and evaluation of an intelligent associate system. *IEEE Trans. on Systems, Man, and Cybernetics*, 25(7):1039–1053, 1995.
- [23] Navin Kartik. Strategic communication with lying costs. *Rev. of Economic Studies*, 76(4):1359–1395, 2009.
- [24] Christopher Kiekintveld, Viliam Lisý, and Radek Píbil. Game-theoretic foundations for the strategic use of honeypots in network security. In *Cyber Warfare*, pages 81–101. Springer, 2015.
- [25] Bernard C Levy. Binary and m-ary hypothesis testing. In *Principles of Signal Detection and Parameter Estimation*. Springer Science & Business Media, 2008.
- [26] James Edwin Mahon. The definition of lying and deception. In Edward N. Zalta, editor, *Stanford Encyclopedia of Philosophy*. Winter 2016 edition, 2016.
- [27] Paul R Milgrom. Good news and bad news: Representation theorems and applications. *Bell J. of Econ.*, pages 380–391, 1981.
- [28] Umar Farooq Minhas, Jie Zhang, Thomas Tran, and Robin Cohen. A multifaceted approach to modeling agent trust for effective communication in the application of mobile ad hoc vehicular networks. *IEEE Trans. Systems, Man, and Cybernetics, Part C (Applications and Reviews)*, 41(3):407–420, 2011.
- [29] John F Nash. Equilibrium points in n-person games. *Proc. Nat. Acad. Sci. USA*, 36(1):48–49, 1950.
- [30] Myle Ott, Yejin Choi, Claire Cardie, and Jeffrey T Hancock. Finding deceptive opinion spam by any stretch of the imagination. In *Proc. 49th Annual Meeting Assoc. for Computational Linguistics: Human Language Technologies*, pages 309–319, 2011.
- [31] Jeffrey Pawlick, Sadeh Farhang, and Quanyan Zhu. Flip the cloud: Cyber-physical signaling games in the presence of advanced persistent threats. In *Decision and Game Theory for Security*, pages 289–308. Springer, 2015.
- [32] Jeffrey Pawlick and Quanyan Zhu. Deception by design: Evidence-based signaling games for network defense. In *Workshop on the Econ. of Inform. Security*, Delft, The Netherlands, 2015.
- [33] Jeffrey Pawlick and Quanyan Zhu. A Stackelberg game perspective on the conflict between machine learning and data obfuscation. *IEEE Intl. Workshop on Inform. Forensics and Security*, 2016.
- [34] Jeffrey Pawlick and Quanyan Zhu. Proactive defense against physical denial of service attacks using poisson signaling games. In *Decision and Game Theory for Security*, pages 336–356. Springer, 2017.

- [35] Jeffrey Pawlick and Quanyan Zhu. Strategic trust in cloud-enabled cyber-physical systems with an application to glucose control. *IEEE Trans. Inform. Forensics and Security*, 12(12), 2017.
- [36] Mark L Psiaki, Todd E Humphreys, and Brian Stauffer. Attackers can spoof navigation signals without our knowledge. Here’s how to fight back GPS lies. *IEEE Spectrum*, 53(8):26–53, 2016.
- [37] N. C. Rowe, B. T. Duong, and E. J. Custy. Fake honeypots: A defensive tactic for cyberspace. In *Proc. IEEE Inform. Assurance Workshop*, pages 223–230, June 2006.
- [38] Craig Silverman. This analysis shows how viral fake election news stories outperformed real news on facebook. BuzzFeed News, [Online]. Available: <https://www.buzzfeed.com/craigsilverman/>.
- [39] Joni Uitto, Sampsa Rauti, Samuel Laurén, and Ville Leppänen. A survey on anti-honeypot and anti-introspection methods. In *World Conf. on Inform. Systems and Technologies*, pages 125–134. Springer, 2017.
- [40] Aldert Vrij, Samantha A Mann, Ronald P Fisher, Sharon Leal, Rebecca Milne, and Ray Bull. Increasing cognitive load to facilitate lie detection: The benefit of recalling an event in reverse order. *Law and Human Behavior*, 32(3):253–265, 2008.
- [41] William J Youden. Index for rating diagnostic tests. *Cancer*, 3(1):32–35, 1950.
- [42] Nan Zhang, Wei Yu, Xinwen Fu, and Sajal K Das. gPath: A game-theoretic path selection algorithm to protect tor’s anonymity. In *Decision and Game Theory for Security*, pages 58–71. Springer, 2010.
- [43] Tao Zhang and Quanyan Zhu. Strategic defense against deceptive civilian GPS spoofing of unmanned aerial vehicles. In *Decision and Game Theory for Security*, pages 213–233. Springer, 2017.
- [44] Quanyan Zhu and Tamer Başar. Game-theoretic approach to feedback-driven multi-stage moving target defense. In *Decision and Game Theory for Security*, pages 246–263. Springer, 2013.
- [45] J. Zhuang, V. M. Bier, and O. Alagoz. Modeling secrecy and deception in a multiple-period attacker-defender signaling game. *European J. of Operational Res.*, 203(2):409–418, 2010.